

# Privacy-Preserving Inference in Crowdsourcing Systems

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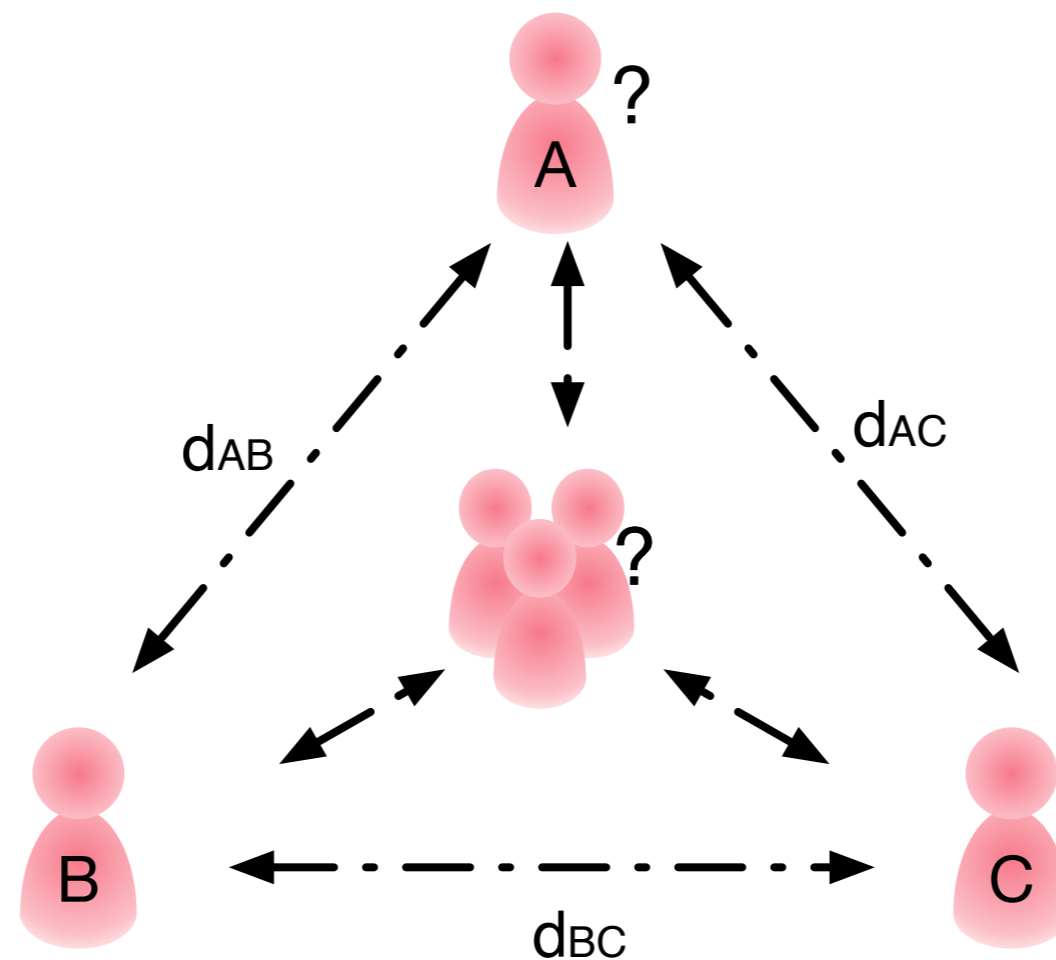
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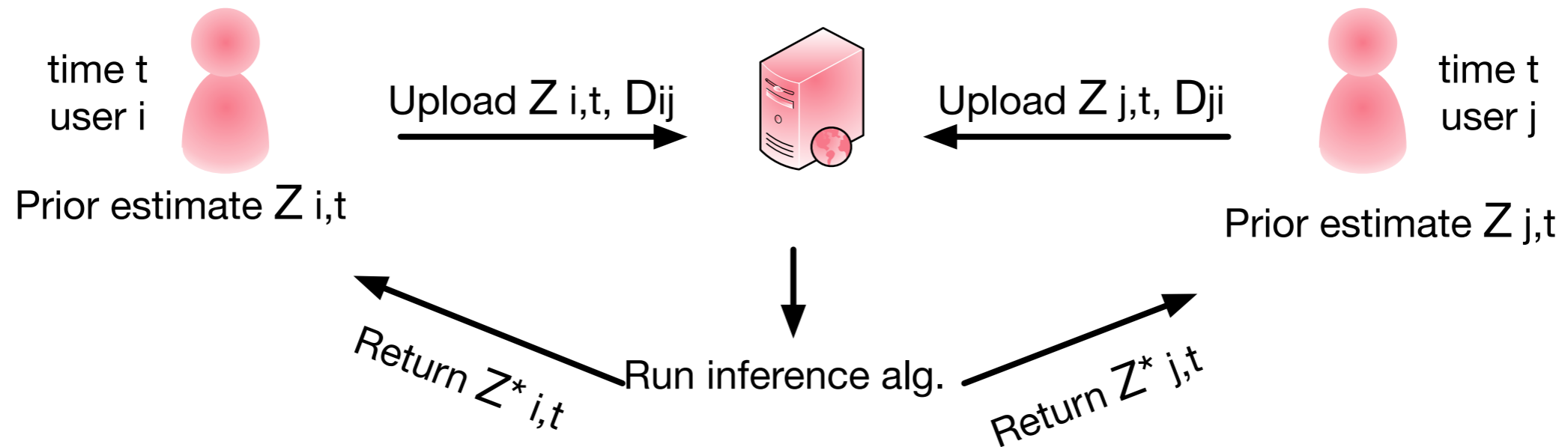
# Localization via Crowdsourcing

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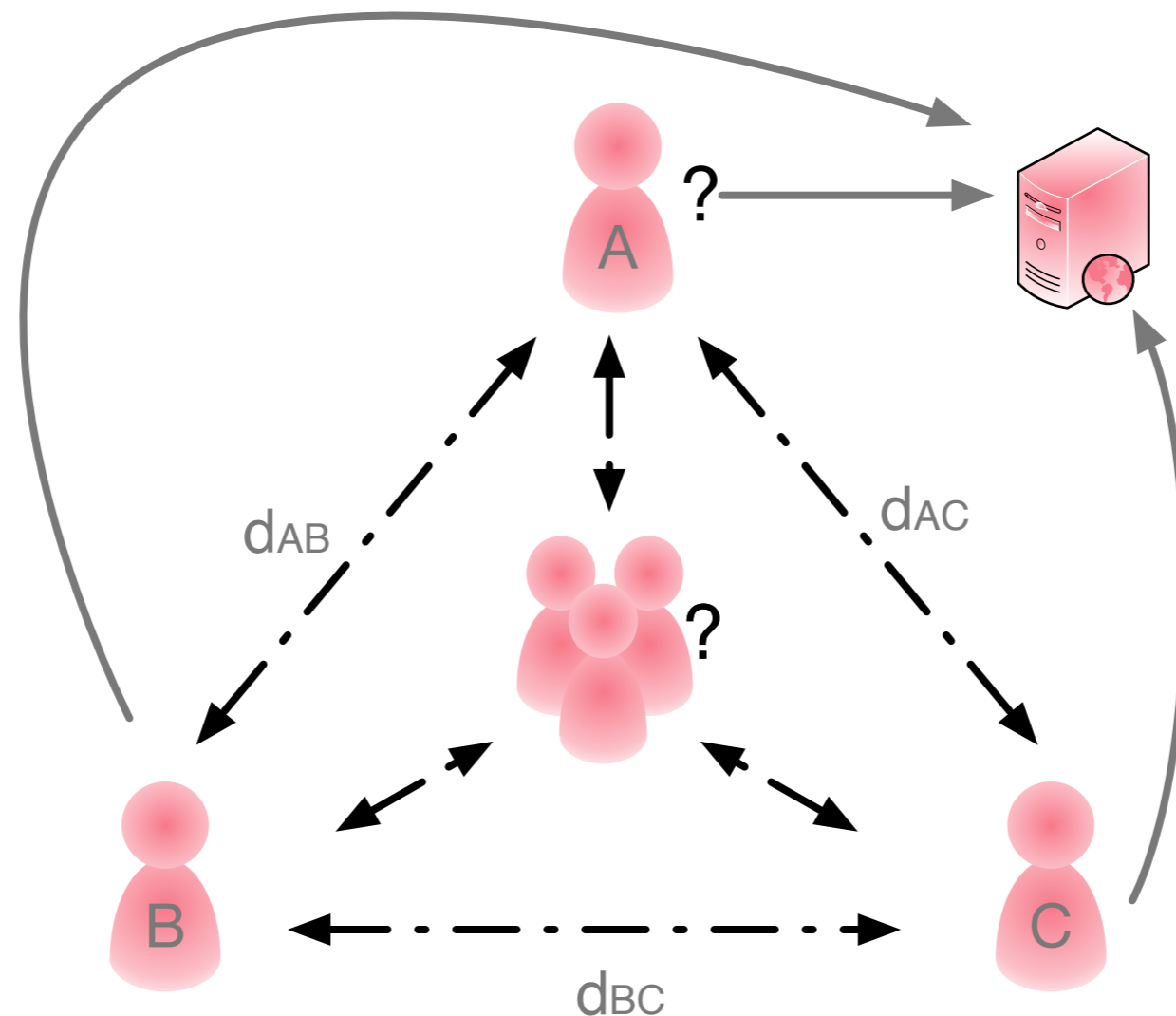
- ▶ In a crowd, some users know about their locations while some don't. With distance observations between them, how to localize each user?

# Localization via Crowdsourcing



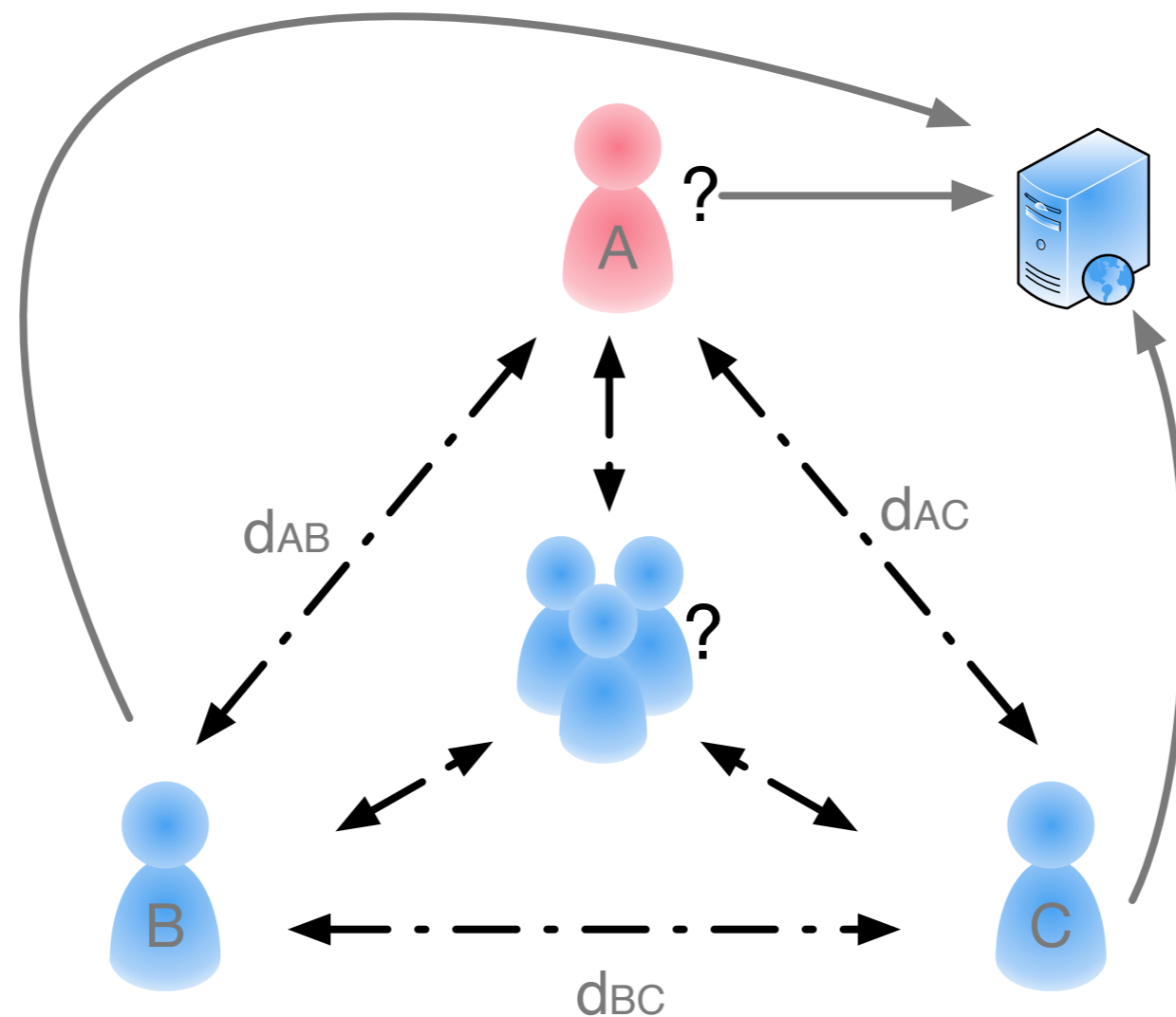
- ▶ Each user sends their prior estimates and distance observations to a central server, who returns the most likely position for each.
- ▶ What if users would like to keep their locations private?

# Privacy-Preserving Localization



- ▶ In a crowd, some users know about their locations while some don't. With distance observations between them, **how to localize each user without breaching privacy?**

# Privacy-Preserving Localization



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# Particle Representation

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- ▶ User's Location

- ▶ A user's location is represented by a set of particles  $\mathbf{Z}_{i,t} = \{z_1, \dots, z_R\}$ ,  $\mathbf{Z}_t = \{\mathbf{Z}_{1,t}, \dots, \mathbf{Z}_{N,t}\}$ .

- ▶ At time  $t$ , the server finds the most likely distribution of  $\mathbf{Z}_t$  given  $\mathbf{Z}_{t-1}$  and  $\mathbf{D}$ .

$$\mathbf{Z}_t^* = \arg \max_{\mathbf{Z}_t} P(\mathbf{Z}_t | \mathbf{Z}_{t-1}, \mathbf{D}).$$

# First Attempt

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- ▶ To encrypt all particles and run the inference in the encrypted domain.

However, encrypted operations are constrained.

# Particle Representation

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- ▶ User's Location

- ▶ A user's location is represented by a set of particles  $\mathbf{z}_{i,t} = \{z_1, \dots, z_R\}$ . Each particle is associated with a weight  $\{w_1, \dots, w_R\}$ .
- ▶ For example, if the location estimate is  $\{z_1, z_2, z_3\}$  with probabilities  $\{0.6, 0.2, 0.2\}$ , then the location is more likely to be  $z_1$  than  $z_3$ .



# Particle Representation

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- ▶ Users upload each particle's weight  $\{E(W_1), \dots, E(W_R)\}$  and distance observations to others  $E(D)$  in **encryption**.
- ▶ Server updates each particle's **weight**.

# Privacy-Preserving Inference

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- ▶ Server computes partial information  $C_{i,r}$  for each particle  $r$  of each user  $i$  ( $j$  is observed by  $i$ ):

$$\begin{aligned} C_{i,r} &= \prod_{j \in \mathcal{N}(i)} \prod_{s \in \{1, \dots, R\}} E_{pk}(\ln w_{j,s}) \cdot E_{pk}(d(z_{i,r}, z_{j,s})^2)^{-\frac{1}{2\sigma^2}} \\ &\quad \cdot E_{pk}(D_{ij})^{\frac{d(z_{i,r}, z_{j,s})}{\sigma^2}} \cdot E_{pk}(D_{ij}^2)^{-\frac{1}{2\sigma^2}} \\ &= E_{pk} \left[ \sum_{j \in \mathcal{N}(i)} \sum_{s \in \{1, \dots, R\}} (\ln w_{j,s} - (d(z_{i,r}, z_{j,s}) - D_{ij})^2 / 2\sigma^2) \right]. \end{aligned}$$

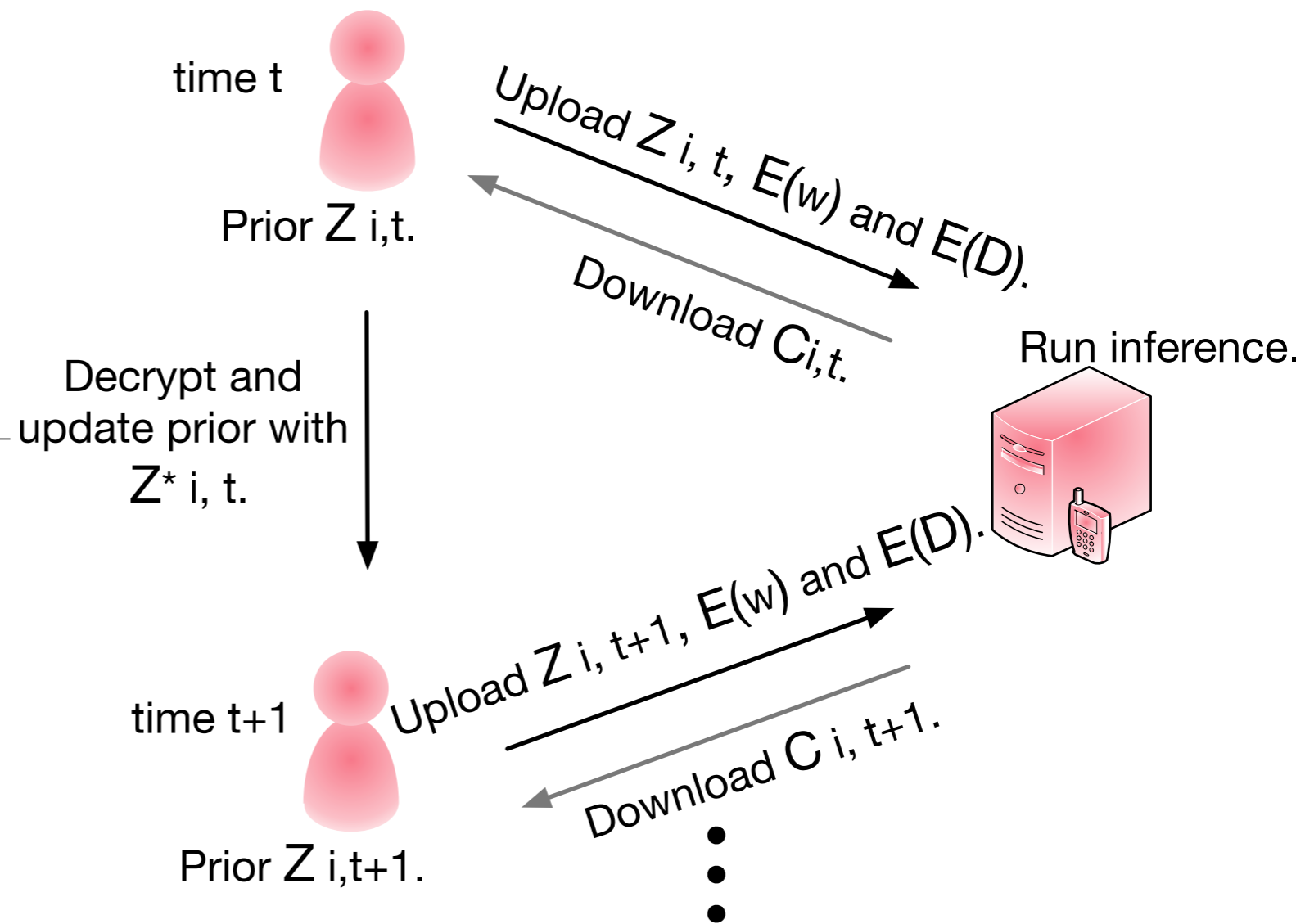
# Privacy-Preserving Inference

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- ▶ With secret key  $sk$ , user  $i$  updates the weight  $w_{i,r}$  for its particle  $r$  ( $d_{js}$  is the calculated distance between particle  $s$  of user  $j$  and particle  $r$  of user  $i$ ):

$$\begin{aligned} w_{i,r}^k &= w_{i,r}^{k-1} \exp[E_{sk}(c_{i,r})] \\ &= w_{i,r}^{k-1} \exp\left[\sum_{j \in \mathcal{N}(i)} \sum_{s \in \{1, \dots, R\}} (\ln w_{j,s} - (d_{js} - D_{ij})^2 / 2\sigma^2)\right] \\ &= w_{i,r}^{k-1} \prod_{j \in \mathcal{N}(i)} \prod_{s \in \{1, \dots, R\}} \exp(\ln w_{j,s} - (d_{js} - D_{ij})^2 / 2\sigma^2) \\ &= w_{i,r}^{k-1} \prod_{j \in \mathcal{N}(i)} \prod_{s \in \{1, \dots, R\}} w_{j,s} \cdot \exp\left(-\frac{(d_{js} - D_{ij})^2}{2\sigma^2}\right) \\ &\simeq w_{i,r}^{k-1} \prod_{j \in \mathcal{N}(i)} \prod_{s \in \{1, \dots, R\}} \Pr(z_{i,r}, z_{j,s} | D_{ij,t}). \end{aligned}$$

# Privacy-Preserving Localization with Crowdsourcing



But, with  $R$  particles, adversary can still guess correct location with Prob.  $1/R$ .

# Data Perturbation

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- ▶ Idea: perturb  $\mathbf{Z}_{i,t} = \{z_1, \dots, z_R\}$  as  $\mathbf{Y}_{i,t} = \{y_1, \dots, y_R\}$ .
- ▶ Perturbation: add Gaussian noise  $\mathcal{N}(0, \sigma^2)$  to  $\mathbf{Z}_{i,t}$  that satisfies location differential privacy.

# Privacy Definition

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► Location Differential Privacy:

A mechanism  $M$  satisfies  $(\epsilon, \delta)$ -differential privacy iff for all  $z, z'$  that are  $d(z, z')$  apart:

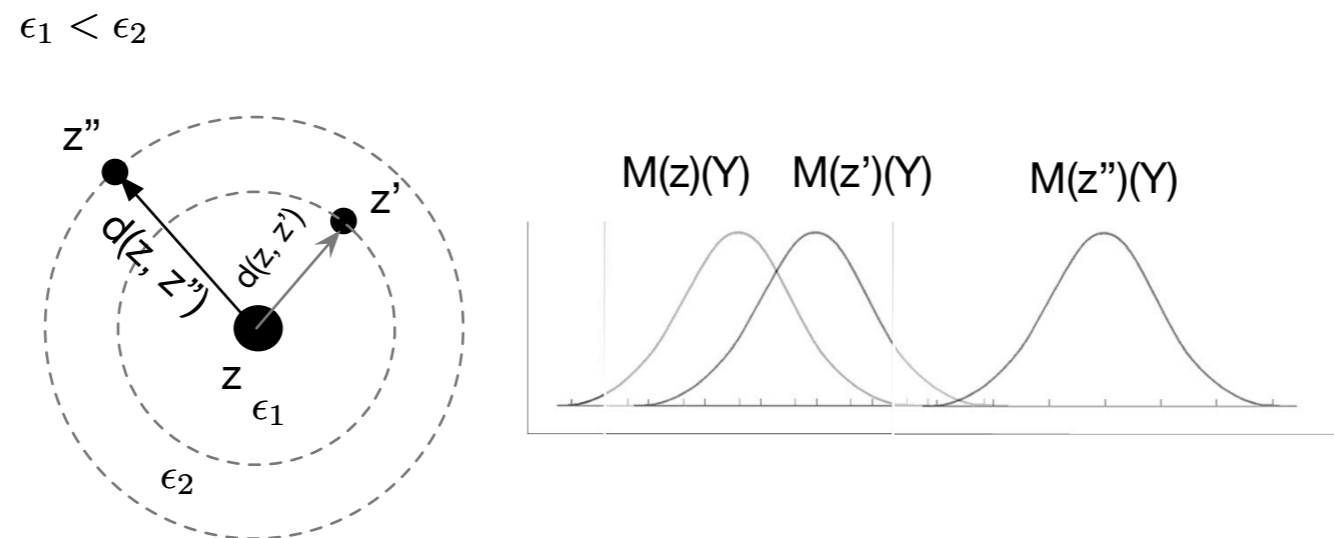
$$\Pr[M(z) \in Y] \leq e^\epsilon \Pr[M(z') \in Y] + \delta,$$

$$\text{and } \epsilon = \rho d^2(z, z') + 2\sqrt{\rho \log(1/\delta)} d(z, z'),$$

where  $\rho$  is a constant specific to the perturbation mechanism we adopt.

# Interpretation of Privacy Definition

- ▶ Location Differential Privacy: the projected distributions of all the points within the same dotted circle are at most  $\epsilon$  apart from each other.



- ▶ As the distance between the two locations is smaller,  $\epsilon$  is smaller, indicating that it is harder to distinguish the two locations, i.e., higher privacy level.



# Privacy Definition

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## ► User Differential Privacy

If we report  $Z = (z_1, \dots, z_R)$  as  $Y = (y_1, \dots, y_R)$ , then the probability of reporting  $Y$  given  $Z$  is:

$$Pr[\mathbf{M}(Z) \in \mathbf{Y}] = \prod_i Pr[M(z_i) \in Y].$$

The user enjoys  $(\epsilon', \delta)$ -differential privacy with

$$\epsilon' = \rho R d^2(Z, Z') + 2\sqrt{\rho \log(1/\delta) R d^2(Z, Z')}.$$

# Perturbed Private Inference

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- ▶ Collecting  $\mathbf{Y}$ , the **server** computes the pairwise distances between each pair of perturbed particles as:

$$\tilde{d}(y, y') = \sqrt{\|y - y'\|_2^2 - 4\sigma^2}.$$

How can we guarantee the inference result the same  
with the unperturbed case?

# Privacy and Utility Analysis

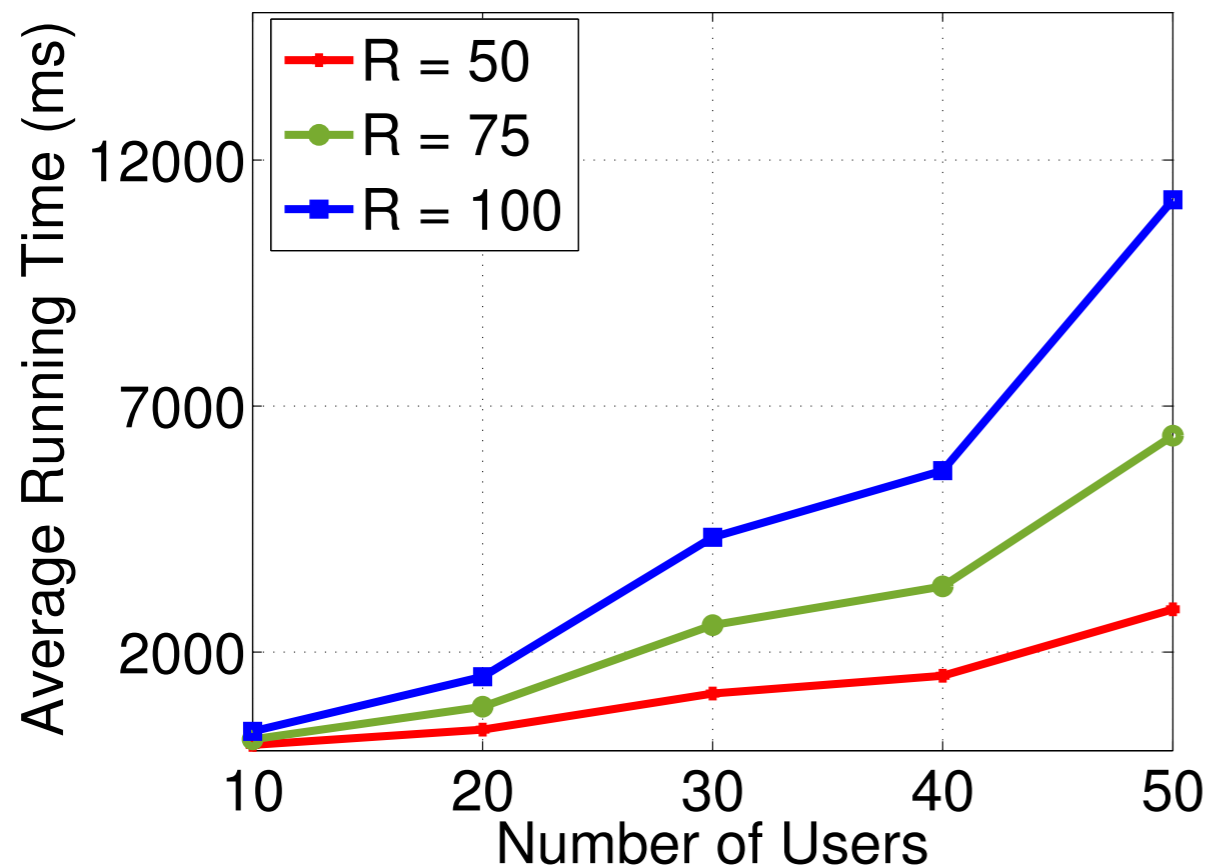
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- ▶ Utility results: We proved  $\tilde{d}(y, y')$  is an unbiased estimator of  $d(z, z')$
- ▶ Privacy guarantee: We proved our perturbation scheme satisfies location differential privacy and user differential privacy. Compared to previous work, we improve the privacy level by  $\sqrt{R}$  with the same utility level.

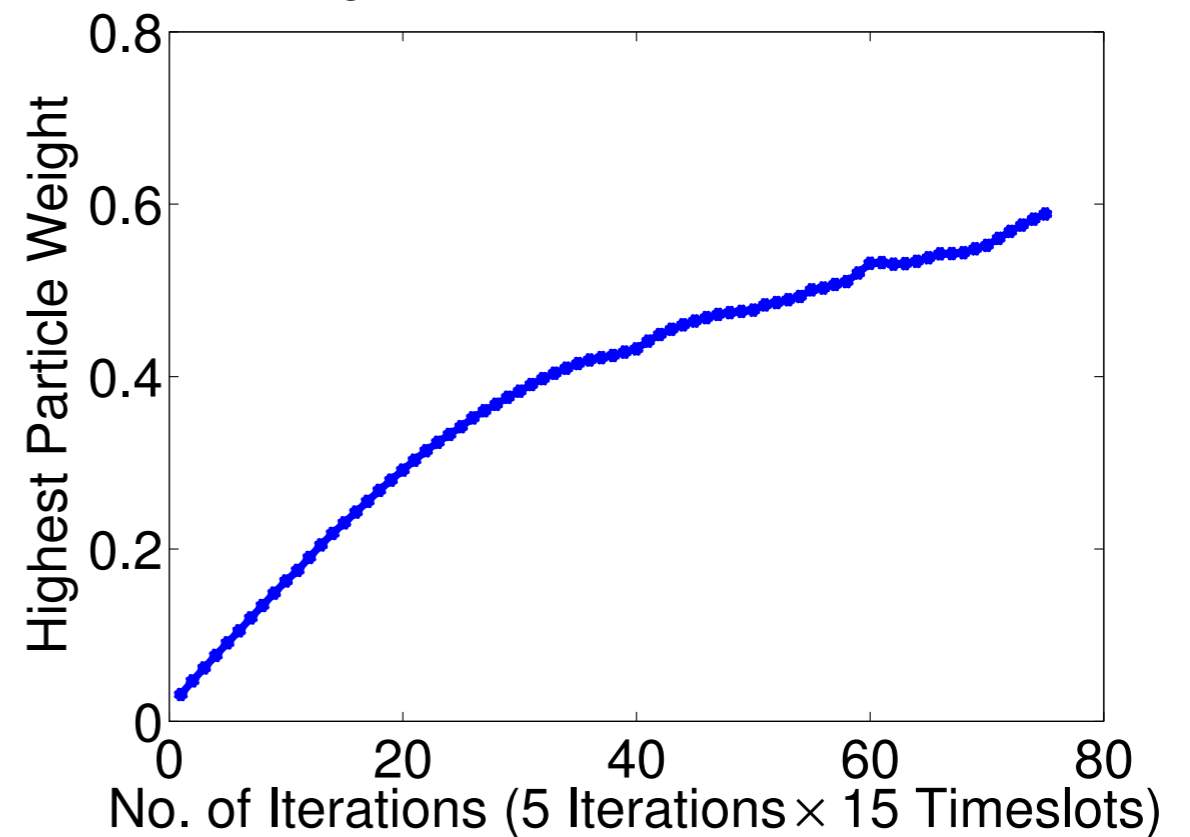
# Performance Evaluation

## ► Overhead

Running Time of the MAP Inference

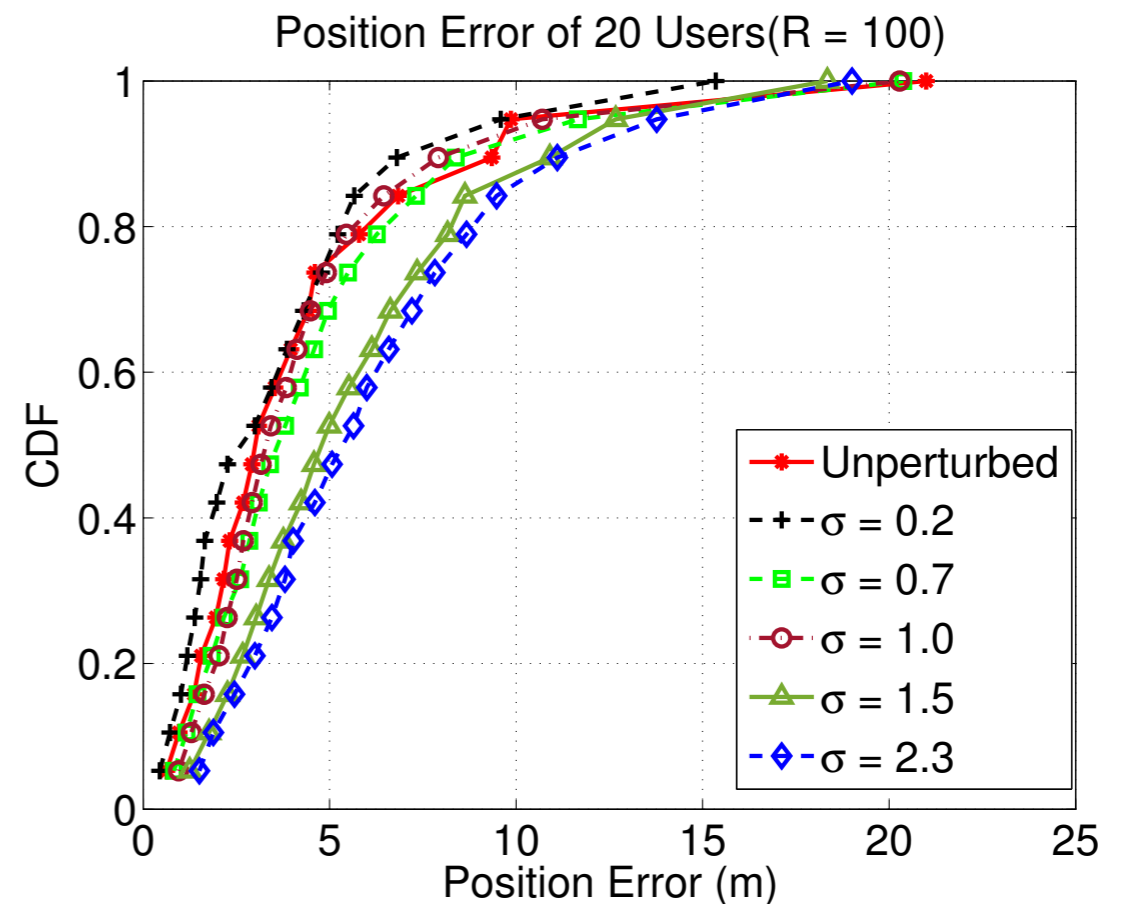
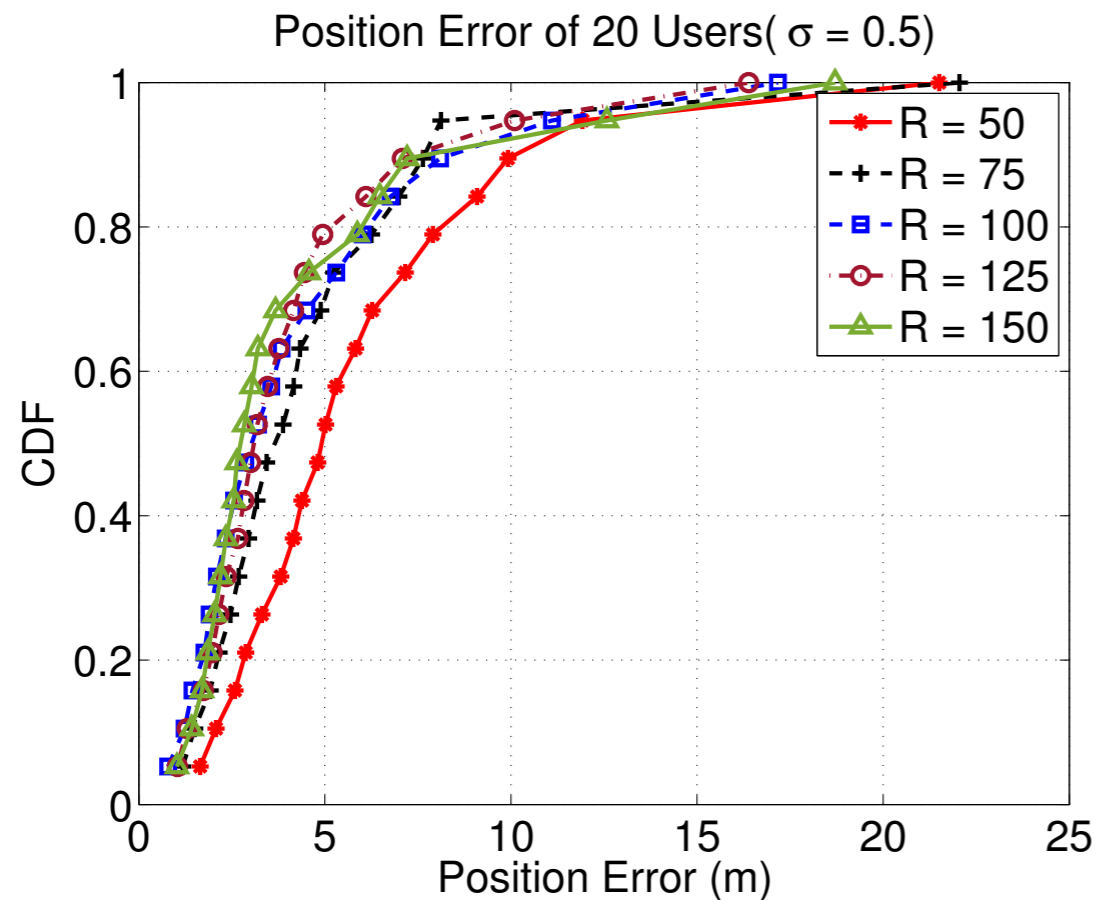


Convergence of the Particle Distribution



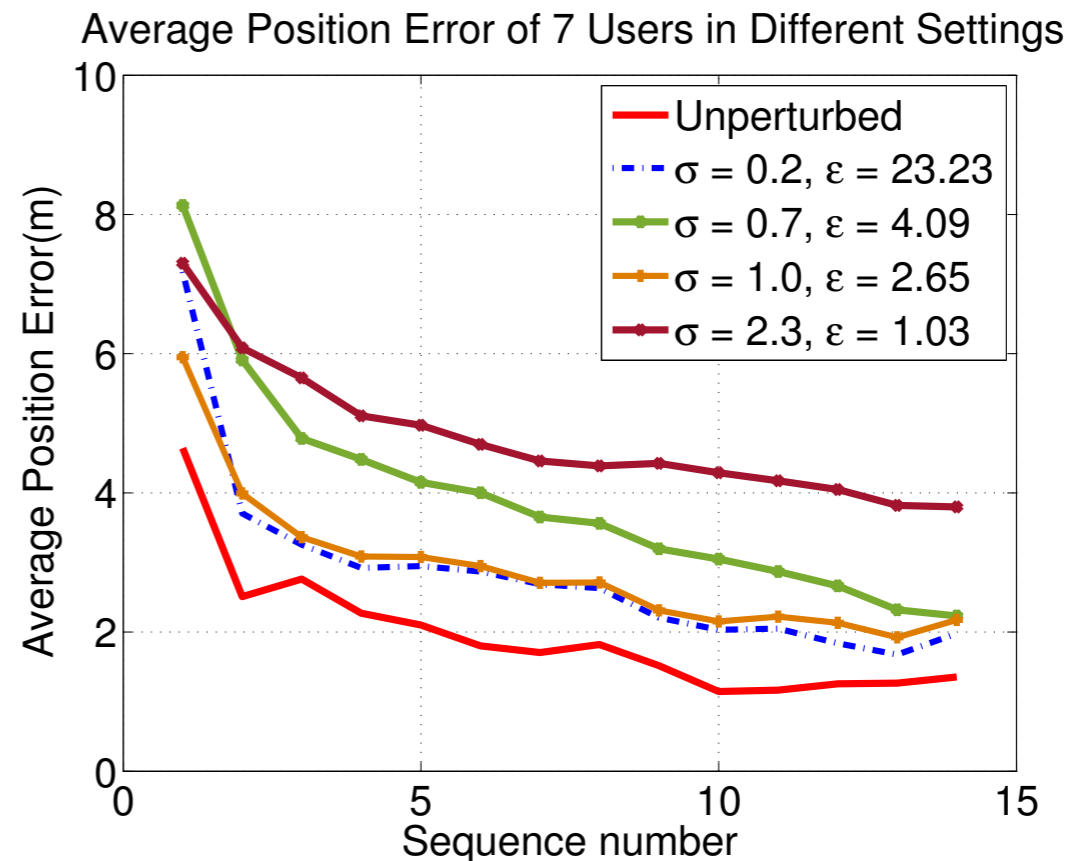
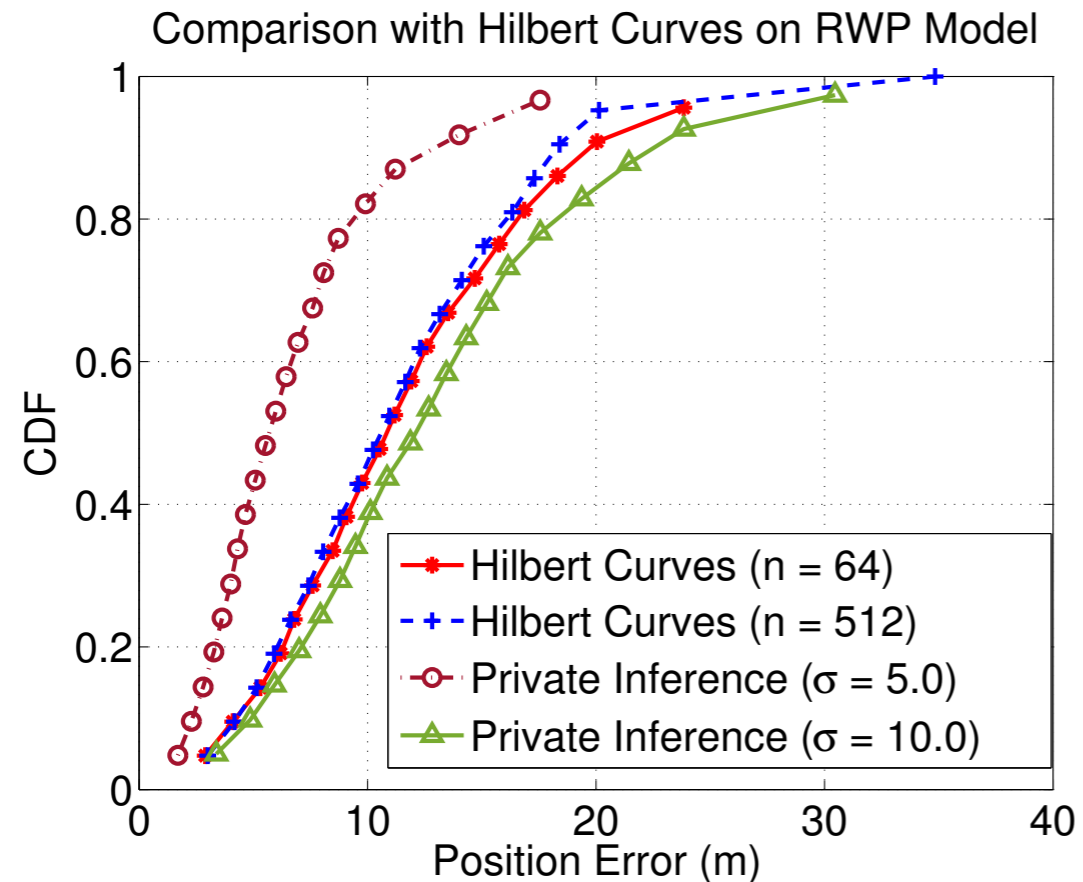
# Performance Evaluation

- ▶ Simulation results using random way point (RWP) model.



# Performance Evaluation

- ▶ Comparison experiment and real-world experimental results.



Thank you!